

$$\left| \iint_D P \vec{n} dS \right| = \rho_s W L h g \sin \theta$$

I chose a coordinate system where \vec{n} can be equal to the unit vector \vec{k} , then I solve the double integral

$$\int_{y=0}^h \int_{x=0}^W \rho_l g (H - h - y \cos \theta) \vec{k} \, dx \, dy = W \left(\rho_l g (H - h) h - \frac{\rho_l g h^2 \cos \theta}{2} \right)$$

Equate to the first expression I had

$$W \left(\rho_l g (H - h) h - \frac{\rho_l g h^2 \cos \theta}{2} \right) = \rho_s W L h g \sin \theta$$

$$\rho_l g (H - h) h - \frac{\rho_l g h^2 \cos \theta}{2} = \rho_s L h g \sin \theta$$

$$\rho_l (H - h) - \frac{\rho_l h \cos \theta}{2} = \rho_s L \sin \theta$$

$$A = \rho_l (H - h)$$

$$B = \frac{\rho_l h}{2}$$

$$C = \rho_s L$$

$$A + B \frac{\sin 2\theta}{2 \sin \theta} = C \sin \theta$$

$$A \sin \theta + \frac{B}{2} \sin 2\theta = C \sin^2 \theta$$

$$2B \sin 2\theta = (C - A) \sin^2 \theta$$