

$$\left| \int \vec{r} \times d\vec{F} \right| = \rho_s WL \frac{h^2}{2} g \sin \theta$$

$$\int \vec{r} \times d\vec{F} = \int \vec{r} \times P \vec{n} dS$$

$$\int y \hat{j} \times \hat{k} P dS = \int \hat{i} y P dS$$

$$\int_{y=0}^h \int_{x=0}^w \rho_l g (H - h + y \cos \theta) y \hat{i} \, dx \, dy = W \left(\rho_l g (H - h) \frac{h^2}{2} + \frac{\rho_l g h^3 \cos \theta}{3} \right)$$

$$W \left(\rho_l g (H - h) \frac{h^2}{2} + \frac{\rho_l g h^3 \cos \theta}{3} \right) = \rho_s WL \frac{h^2}{2} g \sin \theta$$

$$\frac{\rho_l g (H - h)}{2} + \frac{\rho_l g h \cos \theta}{3} = \frac{\rho_s L g \sin \theta}{2}$$

$$3\rho_l (H - h) + 2\rho_l h \cos \theta = 3\rho_s L \sin \theta$$

$$A = 3\rho_l (H - h)$$

$$B = 2\rho_l h$$

$$C = 3\rho_s L$$

$$A + B \cos \theta = C \sin \theta$$

$$A + B \cos \theta = C \frac{\cos 2\theta}{2 \cos \theta}$$

$$A \cos \theta + B \cos^2 \theta = \frac{C}{2} \cos 2\theta$$

$$A \cos \theta + B \cos^2 \theta = \frac{C}{2} (2 \cos^2 \theta - 1)$$

$$A \cos \theta + B \cos^2 \theta - C \cos^2 \theta = -\frac{C}{2}$$

$$(B - 2C) \cos^2 \theta + A \cos \theta + \frac{C}{2} = 0$$