



Calculating Angles

$$\theta + 90^\circ + \theta_4 = 180^\circ \Rightarrow \theta_4 = 90^\circ - \theta$$

$$\theta_4 + \theta_5 = 90^\circ \Rightarrow \theta_5 = 90^\circ - \theta_4$$

$$= 90^\circ - 90^\circ + \theta \Rightarrow \boxed{\theta_5 = \theta}$$

$$90^\circ + \theta + \theta_1 = 180^\circ \Rightarrow \theta_1 = 180^\circ - 90^\circ - \theta$$

$$\theta_1 = 90^\circ - \theta$$

$$\theta_1 + \theta_2 = 90^\circ \Rightarrow \theta_2 = 90^\circ - \theta_1$$

$$= 90^\circ - 90^\circ + \theta \Rightarrow \theta_2 = \theta$$

$$\theta_3 + 90^\circ + \theta_2 = 180^\circ \Rightarrow \theta_3 = 90^\circ - \theta_2 = 90^\circ - \theta \Rightarrow \boxed{\theta_3 = 90^\circ - \theta}$$

Calculating $\vec{W}_y, \vec{W}_x, \vec{a}_x, \vec{a}_y$ in terms of cos and sin

$$\cos(\theta_3) = \frac{\vec{W}_x}{|\vec{W}|} \Rightarrow \vec{W}_x = |\vec{W}| \cdot \cos(\theta_3)$$

$$= m \cdot g \cdot \cos(90^\circ - \theta) \Rightarrow \boxed{\vec{W}_x = m \cdot g \cdot \sin(\theta)} \quad (1)$$

$$\sin(\theta_3) = \frac{\vec{W}_y}{|\vec{W}|} \Rightarrow \vec{W}_y = |\vec{W}| \cdot \sin(\theta_3)$$

$$\Rightarrow \vec{W}_y = m \cdot g \cdot \sin(90^\circ - \theta) \Rightarrow \boxed{\vec{W}_y = m \cdot g \cdot \cos(\theta)} \quad (2)$$

$$\cos(\theta_5) = \frac{\vec{a}_x}{|\vec{a}|} \Rightarrow \vec{a}_x = |\vec{a}| \cdot \cos(\theta_5) = |\vec{a}| \cdot \cos(\theta)$$

$$\Rightarrow \boxed{\vec{a}_x = |\vec{a}| \cdot \cos(\theta)} \quad (3)$$

$$\boxed{\vec{a}_y = |\vec{a}| \cdot \sin(\theta)} \quad (4)$$

Newton's Law

$$\vec{\Sigma F}_x = m \cdot \vec{a}_x \Rightarrow \vec{W}_x = m \vec{a}_x \Rightarrow m \cdot g \cdot \sin(\theta) = m |\vec{a}| \cdot \cos(\theta)$$

$$\Rightarrow g \cdot \sin(\theta) = |\vec{a}| \cdot \cos(\theta) \Rightarrow |\vec{a}| = g \frac{\sin(\theta)}{\cos(\theta)}$$

$$\Rightarrow |\vec{a}| = g \cdot \tan(\theta) \quad (5)$$

$$\vec{\Sigma F}_y = m \cdot \vec{a}_y \Rightarrow \cancel{m \cdot g} \cdot \vec{W}_y + \cancel{m \cdot g} + \vec{T} = m \cdot \vec{a}_y$$

$$\Rightarrow \cancel{m \cdot g \cdot \cos(\theta)} + |\vec{a}| \cdot m \cdot \sin(\theta) + |\vec{T}| = m$$

$$\Rightarrow m \cdot g \cdot \cos(\theta) + |\vec{T}| = m \cdot |\vec{a}| \cdot \sin(\theta)$$

$$\Rightarrow |\vec{T}| = m \cdot |\vec{a}| \cdot \sin(\theta) - m \cdot g \cdot \cos(\theta)$$

$$\Rightarrow |\vec{T}| = m \cdot g \cdot \tan(\theta) \cdot \sin(\theta) - m \cdot g \cdot \cos(\theta)$$

$$\Rightarrow |\vec{T}| = m \cdot g [\tan(\theta) \cdot \sin(\theta) - \cos(\theta)] \quad (6)$$