

$$\rho = \rho_0 \cos \frac{\pi z}{z_0}$$

$$\begin{array}{c|c|c} \rho=0 & \rho = \rho_0 \cos \frac{\pi z}{z_0} & \rho=0 \\ -z_0 & b & z_0 \end{array}$$

$$\nabla^2 \Phi = 0 \quad z \geq z_0$$

$$\nabla^2 \Phi = 0 \quad z \leq -z_0$$

$$\nabla^2 \Phi = \frac{\rho}{\epsilon_0} \quad |z| < z_0$$

$$\frac{\partial \Phi}{\partial z} = 0$$

$$\frac{\partial \Phi}{\partial z} = 0$$

$$-\frac{\partial \Phi}{\partial z} = \frac{\rho}{\epsilon_0}$$

$$C + \frac{\partial I}{\partial z} \quad zC + D = \Phi$$

$$zC + D' = \Phi$$

$$-\frac{\rho_0 \cos \frac{\pi z}{z_0}}{\epsilon_0} = \frac{\partial \Phi}{\partial z}$$

$$-\frac{z_0}{\pi} \frac{\rho_0 \sin \frac{\pi z}{z_0}}{\epsilon_0} = \frac{\partial \Phi}{\partial z}$$

$$+\frac{z_0^2 \rho_0 \cos(\frac{\pi z}{z_0})}{\pi^2 \epsilon_0} + zC + D = \Phi$$

Because infinite Charge distb  $\Phi(z=\infty) \neq 0$

BC's

Set  $\Phi(z=0) = 0$

$$\Phi_1 = \Phi_0 \quad E_1 = E_0$$

$$\Phi_0 = \Phi_1 \quad E_0 = E_1$$

I have 5 BC's and 6 unknowns

$$+\frac{z_0^2 \rho_0 \cos(\frac{\pi z}{z_0})}{\pi^2 \epsilon_0} + zC + D = \Phi$$

$$\Phi(z=0) = 0 \quad \frac{z_0^2 \rho_0}{\pi^2 \epsilon_0} + 0 + D = 0$$

$$D = -\frac{z_0^2 \rho_0}{\pi^2 \epsilon_0}$$

$$\frac{z_0^2 \rho_0}{\pi^2 \epsilon_0} \cos(\frac{\pi z}{z_0}) + zC - \frac{z_0^2 \rho_0}{\pi^2 \epsilon_0} = \Phi$$

I understand that we can choose our potential reference point if at  $\infty$  Potential  $\neq 0$

In the solution they set  $E(z=0) = 0$  I don't understand where this boundary condition came from

Is E field like potential? Can we choose a reference point?