

Calculating Angles

$$\angle \hat{B}A: \theta_1 + 90^\circ + \theta(t) = 180^\circ$$

$$\Rightarrow \boxed{\theta_1 = 90^\circ - \theta(t)}$$

$$\theta_1 + \theta_2 = 90^\circ \Rightarrow \theta_2 = 90^\circ - 90^\circ + \theta(t)$$

$$\boxed{\theta_2 = \theta(t)}$$

$$\angle \hat{O}A: \theta_3 + 90^\circ + \theta(t) = 180^\circ$$

$$\Rightarrow \boxed{\theta_3 = 90^\circ - \theta(t)}$$

$$\theta_3 + \theta_4 = 90^\circ \Rightarrow \theta_4 = 90^\circ - 90^\circ + \theta(t)$$

$$\Rightarrow \boxed{\theta_4 = \theta(t)}$$

$$\angle \hat{A}O: \theta_4 + 90^\circ + \theta_5 = 180^\circ \Rightarrow \theta_5 = 90^\circ - \theta_4$$

$$\Rightarrow \boxed{\theta_5 = 90^\circ - \theta(t)}$$

Analysing vectors to T and N axis

$$\cos(\theta_5) = \frac{W_T}{|W|} \Rightarrow W_T = m \cdot g \cdot \cos[90^\circ - \theta(t)] \Rightarrow \boxed{W_T = m \cdot g \cdot \sin[\theta(t)]} \quad (2)$$

$$\sin(\theta_5) = \frac{W_N}{|W|} \Rightarrow W_N = m \cdot g \cdot \sin[90^\circ - \theta(t)] = -m \cdot g \cdot \sin(\theta(t) - 90^\circ)$$

$$\Rightarrow \boxed{W_N = -m \cdot g \cdot \cos(\theta(t))} \quad (2)$$

$$\cos(\theta_2) = \frac{a_T}{|\vec{a}|} \Rightarrow \boxed{a_T = |\vec{a}| \cdot \cos(\theta(t))}$$

$$\sin(\theta_2) = \frac{a_N}{|\vec{a}|} \Rightarrow \boxed{a_N = |\vec{a}| \cdot \sin(\theta(t))}$$

Είναι σωστά

σιν και κοσ

και οι μόν

αίτια είναι

εδώ σιγά

$a_T = \frac{v^2}{L}$ κανονικά

$$\vec{\Sigma F}_T = m \cdot a_T \Leftrightarrow W_T = m \cdot a_T \Leftrightarrow m \cdot g \cdot \sin(\theta(t)) = m \cdot a_T$$

$$a_T = g \cdot \sin(\theta(t)) \quad (3)$$

$$\vec{\Sigma F}_N = m \cdot a_N \Leftrightarrow T + W_N = m \cdot a_N$$

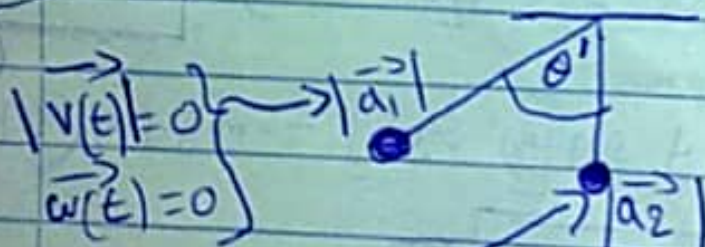
$$\Leftrightarrow T - m \cdot g \cdot \cos(\theta(t)) = m \cdot \frac{|\vec{v}|^2}{L}$$

$$\Rightarrow T = m \cdot \frac{|\vec{v}|^2}{L} + m \cdot g \cdot \cos(\theta(t))$$

$$\Rightarrow T = m \left[\frac{|\vec{v}|^2}{L} + g \cdot \cos(\theta(t)) \right] \quad (4)$$

\vec{T} εφαρμάξε και στο εναυ εκκρεμές $\vec{v}(t)$
 όπου και στο χρονό, δεν είναι ανεξαρτητή
 από τον κόρνο να κινώ Α.Δ.Μ.Ε

$$|\vec{a}| = \sqrt{a_T^2 + a_N^2} = \sqrt{g^2 \cdot \sin^2(\theta(t)) + \left[\frac{|\vec{v}|^2}{L} \right]^2}$$



$$\theta' = \theta(t)_{\max}$$

$$|\vec{a}_1| = |\vec{a}_2| \rightarrow \text{δεδομένο}$$

$$|\vec{v}(t)| = v_{\max}$$

$$\omega(t) = \omega_{\max}$$

$$|\vec{a}_1| @ V=0 : |\vec{a}_1| = \sqrt{g^2 \cdot \sin^2(\theta(t)) + 0} = g \sin(\theta(t))$$

$$|\vec{a}_2| @ V=V_{max} : |\vec{a}_2| = \sqrt{g^2 \cdot \sin^2(\theta(t)) + \frac{V_{max}^4}{L^2}}$$

$$|\vec{a}_1| = |\vec{a}_2| \Rightarrow g \cdot \sin[\theta(t)] = \sqrt{g^2 \cdot \sin^2(\theta(t)) + \frac{V_{max}^4}{L^2}}$$

$$\Rightarrow g^2 \cdot \sin^2[\theta(t)] = g^2 \cdot \sin^2(\theta(t)) + \frac{V_{max}^4}{L^2}$$

$$\frac{V_{max}^4}{L^2} = 0 \Rightarrow V_{max} = 0 \quad \text{σ επιέρχο... ΔΕΝ ΟΥΤΕΙ ΠΑΘΕΝΑ!!}$$

As συνθήκη να ται $\dot{\alpha} > 0$:

$$a_T = \frac{\partial |\vec{v}|}{\partial t} \Rightarrow \partial |\vec{v}| = a_T \partial t = g \cdot \sin(\theta(t))$$

$$\int_{v(0)}^{v(t)} \partial |\vec{v}(t)| = \int_0^t g \cdot \sin(\theta(t)) \partial t$$

$$\frac{\partial \theta(t)}{\partial t} = \omega(t) \Rightarrow \partial t = \frac{\partial \theta(t)}{\omega(t)}$$

$$\rightarrow v(t) - v(0) = g \int_{\theta(0)}^{\theta(t)} \sin(\theta(t)) \cdot \frac{\partial \theta(t)}{\omega(t)}$$

$$= \frac{g}{\omega(t)} \int_{\theta(0)}^{\theta(t)} \sin(\theta(t)) \partial \theta(t) = \frac{g}{\omega(t)} \left[-\cos(\theta(t)) \right]_{\theta(0)}^{\theta(t)}$$

$$= \frac{-g}{\omega(t)} \left[\cos(\theta(t)) - \cos(\theta(0)) \right] \Rightarrow \cancel{v(t)} =$$

$$v(t) = \frac{g}{\omega(t)} \cdot \cos(\theta(0)) - \frac{g}{\omega(t)} \cdot \cos(\theta(t)) \quad (5)$$

$$(5) \rightarrow \frac{g}{\omega(t)} \cdot \cos(\theta(t)) = \frac{g}{\omega(t)} \cdot \cos(\theta(0)) - v(t)$$

$$\cos(\theta(t)) = \cos(\theta(0)) - \frac{g \cdot v(t)}{\omega(t)}$$

$$\theta(t) = \cos^{-1} \left[\cos(\theta(0)) - \frac{g \cdot v(t)}{\omega(t)} \right] \quad (6)$$

συνεχίζω ότι $\theta' = \max[\theta(t)]$, $v(t) = 0$
 $a \gg a$ και $\omega(t) = 0$, άρα $\frac{g \cdot 0}{0}$ πρόβλημα!!!

αν όμως βρω $\frac{\partial \theta(t)}{\partial t} = \omega(t)$ είναι καίρι???

Παίρνει και φανερώνω η εξίσωση, κινείται
 ή στα και v και ω και δεν είναι εξαρτημένη
 με t μεσαδιάζει.

Εννοώ καίρι άρα:

$$\text{ποσοστό } |\vec{v}(t)| = \omega(t) \cdot L \quad \text{άρα}$$

$$\theta(t) = \cos^{-1} \left[\cos(\theta(0)) - \frac{g \cdot \omega(t) \cdot L}{\omega(t)} \right]$$

$$\theta(t) = \cos^{-1} \left[\cos(\theta(0)) - g \cdot L \right] \quad \left\{ \begin{array}{l} \text{σταθερά} \\ a > a ??? \end{array} \right.$$

ΛΑΘΟΣ γιατί $\frac{\partial \theta(t)}{\partial t} = 0$???