

The formula for the covariant vector transformation from the  $R^2$  coordinate system to the  $B$  coordinate system is:

$$V_m^{(B)} = \frac{\partial x^n}{\partial y^m} V_n^{(R^2)}$$

For our example, the vector  $\dot{V} = x^2 e_1 + y^2 e_2$ , where  $e_1$  and  $e_2$  are the basis for  $R^2$ .

Our new coordinate system  $B = f(e_1, e_2)$ ; spanned by

$$b_1 = 2e_1 + 2e_2$$

$$b_2 = e_2$$

To find  $V_1$  in the  $B$  basis in terms of  $V_i$  in  $R^2$ :

$$V_1^{(B)} = \frac{\partial e^i}{\partial b^1} V_i^{(R^2)}$$

$$V_1^{(B)} = \frac{\partial e^1}{\partial (2e_1 + 2e_2)} x^2 + \frac{\partial e^2}{\partial (2e_1 + 2e_2)} x^2$$

$$V_1^{(B)} = 2x^2 + 2y^2$$