

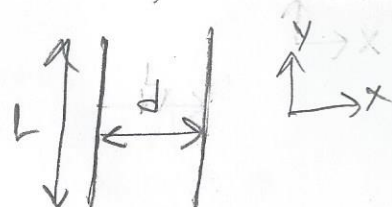
(2)

$$V_x = 0$$

$$V_y = f(x, y, z)$$

$$V_z = 0$$

a)



$$\rho \left[\cancel{\frac{\partial V_y}{\partial t}} + V_x \cancel{\frac{\partial V_x}{\partial x}} + V_y \cancel{\frac{\partial V_y}{\partial y}} + V_z \cancel{\frac{\partial V_z}{\partial z}} \right] = -\frac{\partial p}{\partial y} + \mu \left[\frac{\partial^2 V_y}{\partial x^2} + \cancel{\frac{\partial^2 V_y}{\partial y^2}} + \cancel{\frac{\partial^2 V_z}{\partial z^2}} \right] + \cancel{\rho V_y}$$

$$\mu \frac{\partial^2 V_y}{\partial x^2} - \frac{\partial p}{\partial y} = 0$$

BC

$$V_y(x=0) = 0$$

$$V_y(x=d) = 0$$

$$\frac{\partial^2 V_y}{\partial x^2} - \frac{1}{\mu} \frac{\partial p}{\partial y} = 0$$

$$\frac{\partial^2 V_y}{\partial x^2} = \frac{1}{\mu} \frac{\partial p}{\partial y}$$

$$\frac{\partial V_y}{\partial x} = \frac{1}{\mu} \frac{\partial p}{\partial y} x + C_1$$

$$V_y = \frac{1}{2\mu} \frac{\partial p}{\partial y} x^2 + C_1 x + C_2$$

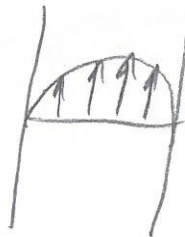
$$V_y^{x=0} = 0 + 0 + C_2$$

$$\Rightarrow C_2 = 0$$

$$0 = \frac{1}{2\mu} \frac{\partial p}{\partial y} d^2 + C_1 d$$

$$C_1 = -\frac{d}{2\mu} \frac{\partial p}{\partial y}$$

$$V_y = \frac{1}{2\mu} \frac{\partial p}{\partial y} x^2 - \frac{d}{2\mu} \frac{\partial p}{\partial y}$$



$$V_y = \frac{1}{2\mu} \frac{\partial p}{\partial y} [x^2 - d^2]$$