



A) FIND the transfer function:  $G(s) = \frac{V_o(s)}{V_i(s)}$

**STEP 1:** Choose a Configuration

$$i_1 > i_2 > i_3$$

## STEP 2: KIRCHHOFF'S VOLTAGE LAW

Loop 1:  $V_{C1} + V_{C2} - V_i = 0$

$$V_{C1} + V_{C2} = V_i$$

$$|V_{C1}| = \frac{\int (i_1 - i_2) dt}{C_1}$$

$$|V_{C2}| = \frac{\int (i_1 - i_2) dt}{C_2}$$

$$\frac{\int (i_1 - i_2) dt}{C_1} + \frac{\int (i_1 - i_2) dt}{C_2} = V_i$$

$$\boxed{\left(\frac{1}{C_1 + C_2}\right) \int (i_1 - i_2) dt = V_i} \quad \text{---(1)}$$

Loop 2:

$$V_{R_1} + V_{R_2} - V_{C_2} - V_{C_1} = 0$$

$$|V_{R_1}| = (i_2 - i_3) R_1$$

$$|V_{R_2}| = (i_2 - i_3) R_2$$

$$|V_{C_2}| = \frac{\int (i_1 - i_2) dt}{C_2}$$

$$|V_{C_1}| = \frac{\int (i_1 - i_2) dt}{C_1}$$

$$(i_2 - i_3) R_1 + (i_2 - i_3) R_2 - \frac{\int (i_1 - i_2) dt}{C_2} - \frac{\int (i_1 - i_2) dt}{C_1} = 0$$

$$\boxed{(R_1 + R_2)(i_2 - i_3) - \left(\frac{1}{C_1 + C_2}\right) \int (i_1 - i_2) dt = 0}$$

-(2)

Loop 3:

$$V_L - V_{R_2} - V_{R_1} = 0$$

$$|V_L| = \frac{L \cdot i_3}{dt}$$

$$|V_{R_2}| = (i_2 - i_3) R_2$$

$$|V_{R_1}| = (i_2 - i_3) R_1$$

$$\frac{L i_3}{dt} - (i_2 - i_3) R_2 - (i_2 - i_3) R_1 = 0$$

$$\boxed{\frac{L i_3}{dt} - (R_1 + R_2)(i_2 - i_3) = 0} \quad -(3)$$

$$|V_o| = |V_{oRT}| - |V_{oCT}|$$

$$|V_{oRT}| = V_i \left( \frac{R_2}{R_1 + R_2} \right)$$

$$|V_{oCT}| = V_i \left( \frac{C_1}{C_1 + C_2} \right)$$

$$|V_o| = V_i \left( \frac{R_2}{R_1 + R_2} \right) - V_i \left( \frac{C_1}{C_1 + C_2} \right)$$

$$|V_o| = V_i \left[ \left( \frac{R_2}{R_1 + R_2} \right) - \left( \frac{C_1}{C_1 + C_2} \right) \right] \quad - (4)$$

~~$$|V_i| = V_o \left[ \left( \frac{R_1 + R_2}{R_2} \right) - \left( \frac{C_1 + C_2}{C_1} \right) \right]$$~~

### STEP 3: Laplace Transform

$$\left( \frac{1}{C_1 + C_2} \right) \int (i_1 - i_2) dt = V_i \quad -(1)$$

$$\rightarrow \left( \frac{1}{C_1 + C_2} \right) \left( \frac{1}{s} \right) (I_1 s - I_2 s) = V_i s \quad -(5)$$

$$\left( (R_1 + R_2)(i_2 - i_3) - \left( \frac{1}{C_1 + C_2} \right) \int (i_1 - i_2) dt \right) = 0 \quad -(2)$$

$$\rightarrow (R_1 + R_2)(I_2 s - I_3 s) - \left( \frac{1}{C_1 + C_2} \right) \left( \frac{1}{s} \right) (I_1 s - I_2 s) = 0 \quad -(6)$$

$$\left( \frac{L i_3}{dt} - (R_1 + R_2)(i_2 - i_3) \right) = 0 \quad -(3)$$

$$\rightarrow L s I_3 s - (R_1 + R_2)(I_2 s - I_3 s) = 0 \quad -(7)$$

$$V_o = V_i \left[ \left( \frac{R_2}{R_1 + R_2} \right) - \left( \frac{C_1}{C_1 + C_2} \right) \right] \quad -(4)$$

$$V_o s = V_i s \left[ \left( \frac{R_2}{R_1 + R_2} \right) - \left( \frac{C_1}{C_1 + C_2} \right) \right] \quad -(8)$$