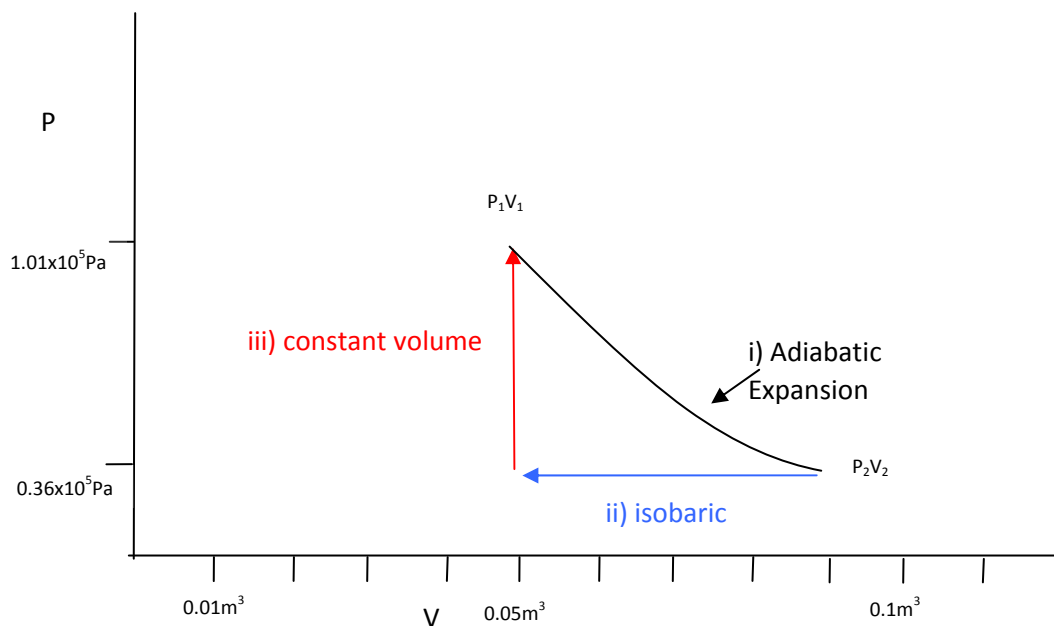


2. 1.0 mol sample of an ideal monatomic gas originally at a pressure of 1 atm undergoes a 3-step process as follows:
- It expands adiabatically from $T_1 = 588 \text{ K}$ to $T_2 = 389 \text{ K}$
 - It is compressed at constant pressure until its temperature reaches $T_3 \text{ K}$
 - It then returns to its original pressure and temperature by a constant volume process.
- Plot these processes on a PV diagram
 - Determine the temperature T_3
 - Calculate the change in internal energy, work done by the gas and heat added to the gas for each of these three processes
 - Calculate the change in internal energy, work done by the gas and heat added to the gas for the complete cycle.



Figures in bold are given data points.

$V_1 = 0.0484 \text{ m}^3$	$T_1 = \mathbf{588 \text{ K}}$	$P_1 = \mathbf{1.01 \times 10^5 \text{ Pa}}$	1 mole, ideal gas, monatomic
$V_2 = 0.0899 \text{ m}^3$	$T_2 = \mathbf{389 \text{ K}}$	$P_2 = 3.59 \times 10^4 \text{ Pa}$	$\gamma = \mathbf{1.66}$

Solve for V_1 using universal gas law:

$$V_1 = \frac{nRT_1}{P_1} \rightarrow V_1 = \frac{1 \text{ M} \cdot 8.314 \text{ J M}^{-1} \text{ K}^{-1} \cdot 588 \text{ K}}{1.01 \times 10^5 \text{ Pa}} \rightarrow V_1 = 0.0484 \text{ m}^3$$

Solve for V_2 using proportionality of temperature and volume during adiabatic process:

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1} \right)^{\gamma-1} \rightarrow \frac{588K}{389K} = \left(\frac{V_2}{0.0484m^3} \right)^{0.66} \rightarrow \left(\frac{588K}{389K} \right)^{\frac{1}{0.66}} = \frac{V_2}{0.0484m^3} \rightarrow 1.5116^{\frac{1}{0.66}} =$$

$$\frac{V_2}{0.0484m^3}$$

$$\rightarrow 1.859 = \frac{V_2}{0.0484m^3} \rightarrow V_2 = 0.0899m^3$$

To solve for P_2 we will use proportionality of temperature and pressure:

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2} \right)^{\gamma} \rightarrow \frac{P_2}{1.01 \times 10^5 Pa} = \left(\frac{0.0484m^3}{0.0899m^3} \right)^{1.66} \rightarrow \frac{P_2}{1.01 \times 10^5 Pa} = 0.35629 \rightarrow P_2 = 3.59 \times 10^4 Pa$$

(ii) It is compressed at constant pressure until its temperature reaches T_3 K

$$P = 3.59 \times 10^4 Pa$$

Using Charles Law: