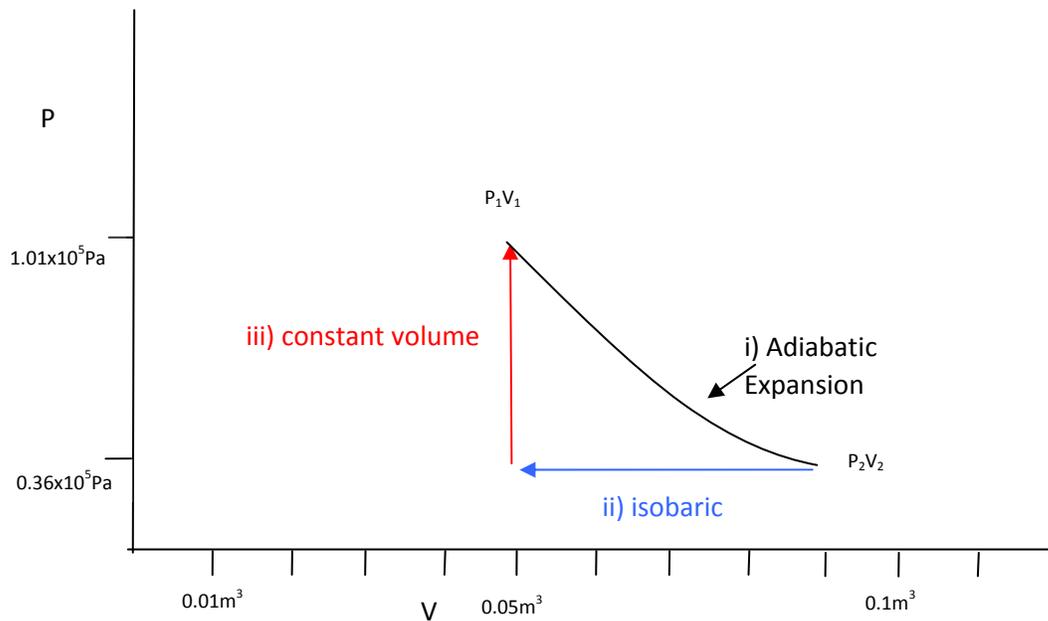


2. 1.0 mol sample of an ideal monatomic gas originally at a pressure of 1 atm undergoes a 3-step process as follows:
- It expands adiabatically from  $T_1 = 588\text{ K}$  to  $T_2 = 389\text{ K}$
  - It is compressed at constant pressure until its temperature reaches  $T_3\text{ K}$
  - It then returns to its original pressure and temperature by a constant volume process.
- Plot these processes on a PV diagram
  - Determine the temperature  $T_3$
  - Calculate the change in internal energy, work done by the gas and heat added to the gas for each of these three processes
  - Calculate the change in internal energy, work done by the gas and heat added to the gas for the complete cycle.



Figures in bold are given data points.

|                          |                              |   |                                      |
|--------------------------|------------------------------|---|--------------------------------------|
| $V_1 = 0.0484\text{m}^3$ | $T_1 = \mathbf{588\text{K}}$ | $P_1 = \mathbf{1.01 \times 10^5\text{ Pa}}$ | <b>1 mole, ideal gas, monoatomic</b> |
| $V_2 = 0.0899\text{m}^3$ | $T_2 = \mathbf{389\text{K}}$ | $P_2 = 3.59 \times 10^4\text{ Pa}$          | $\gamma = \mathbf{1.66}$             |

Solve for  $V_1$  using universal gas law:

$$V_1 = \frac{nRT_1}{P_1} \rightarrow V_1 = \frac{1M \cdot 8.314\text{JM}^{-1}\text{K}^{-1} \cdot 588\text{K}}{1.01 \times 10^5\text{ Pa}} \rightarrow V_1 = 0.0484\text{m}^3$$

Solve for  $V_2$  using proportionality of temperature and volume during adiabatic process:

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1} \rightarrow \frac{588K}{389K} = \left(\frac{V_2}{0.0484m^3}\right)^{0.66} \rightarrow \left(\frac{588K}{389K}\right)^{\frac{1}{0.66}} = \frac{V_2}{0.0484m^3} \rightarrow 1.5116^{\frac{1}{0.66}} = \frac{V_2}{0.0484m^3}$$

$$\rightarrow 1.859 = \frac{V_2}{0.0484m^3} \rightarrow V_2 = 0.0899m^3$$

To solve for  $P_2$  we will use proportionality of temperature and pressure:

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^{\gamma} \rightarrow \frac{P_2}{1.01 \times 10^5 Pa} = \left(\frac{0.0484m^3}{0.0899m^3}\right)^{1.66} \rightarrow \frac{P_2}{1.01 \times 10^5 Pa} = 0.35629 \rightarrow P_2 = 3.59 \times 10^4 Pa$$

(ii) It is compressed at constant pressure until its temperature reaches  $T_3$  K

$$P = 3.59 \times 10^4 Pa$$

Using Charles Law: