

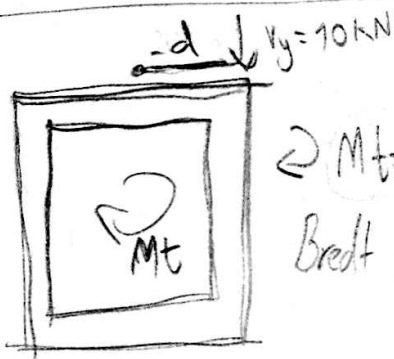
$$\bar{y}_c = \frac{S_x}{A}$$

$$A_{\text{TOTAL}} = 40(10) + 5(85) + 5(85) + 5(40) = 1450 \text{ mm}^2$$

$$S_{x_{\text{TOTAL}}} = 400(95) + 425(50) + 425(50) + 200(2.5) = 81,000 \text{ mm}^3$$

$$\bar{y}_c = \frac{81,000}{1,450} = 55.86 \text{ mm}$$

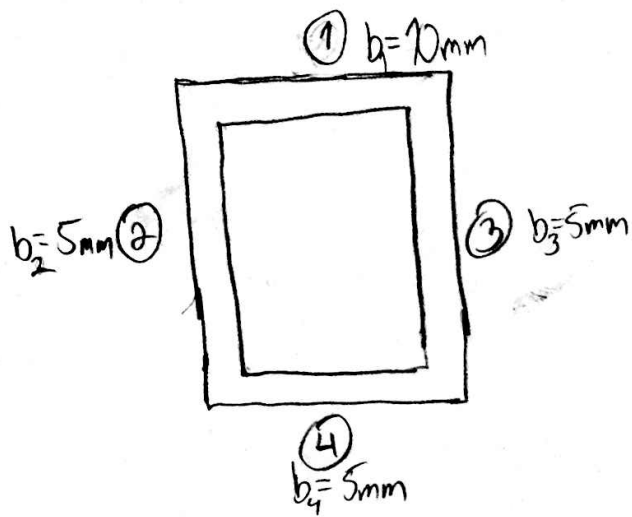
$$\text{Centroid} = (\bar{x}, \bar{y}) = (0, 55.86)$$



$$M_t = Vd = 10(20) = 200 \text{ kN}\cdot\text{mm} = 200 \text{ N}\cdot\text{cm}$$

$$\text{Bredt formula for torsion: } \tau_z = \frac{M_t}{2\Omega b}$$

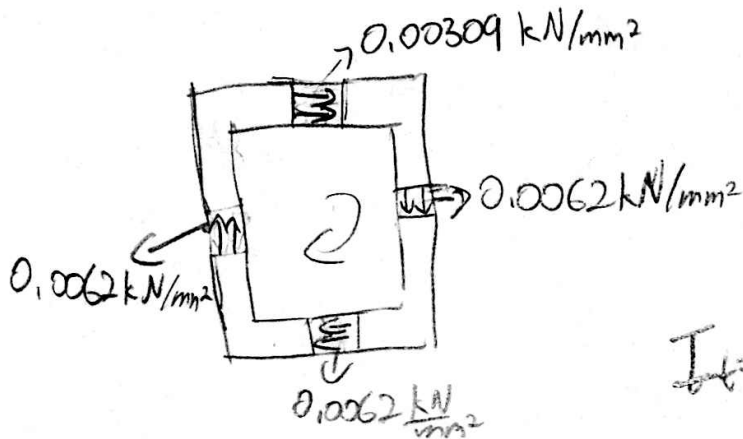
$$\Omega = \text{Area of the frame} = (92.5)(35) = 3237.5 \text{ mm}^2$$



$$M_t = 200 \text{ kN}\cdot\text{mm} \quad \Omega = 3237.5 \text{ mm}^2$$

$$\tau_{z1} = \frac{M_t}{2\Omega b_1} = \frac{200}{2(3237.5)(10)} = 0.00309 \frac{\text{kN}}{\text{mm}^2}$$

$$\tau_{z2} = \tau_{z3} = \tau_{z4} = \frac{200}{2(3237.5)(5)} = 0.0062 \frac{\text{kN}}{\text{mm}^2}$$



$$\tau_{z\max} = \frac{M_t \cdot b}{I_t}$$

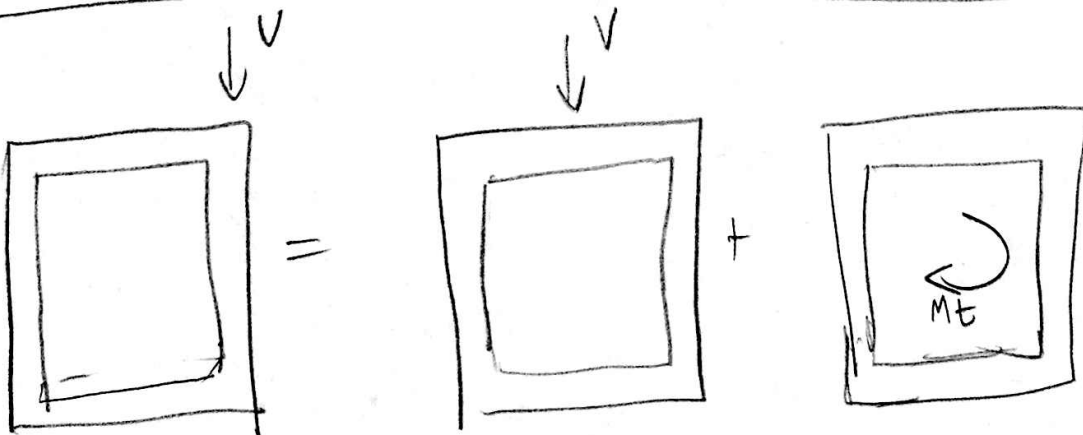
$$I_t = \frac{1}{3} E a b^3 = \frac{1}{3} \left[40(10^3) + 85(5^3) + 85(5^3) + 40(5^3) \right]$$

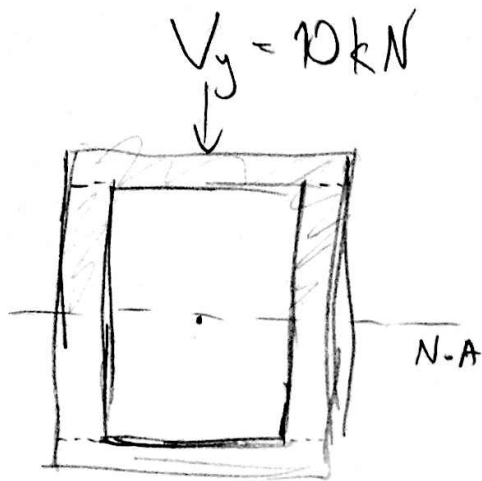
$$= \frac{1}{3} (40,000 + 10,625 + 10,625 + 5,000)$$

$$= 20583.33 \text{ mm}^4$$

$$\tau_z(b=10) = \frac{200}{20583.33} \times 10 = 0.097 \text{ kN/mm}^2$$

$$\tau_z(b=5) = \frac{200}{20583.33} \times 5 = 0.049 \text{ kN/mm}^2$$





$$\tau_{N.A} = \frac{VQ}{Ib} \dots V = 10 \text{ kN}$$

$$N.A = 55.86$$

$$\tau_{N.A} = \frac{10 \times 17,656.6}{1,763,609.93 \times 10}$$

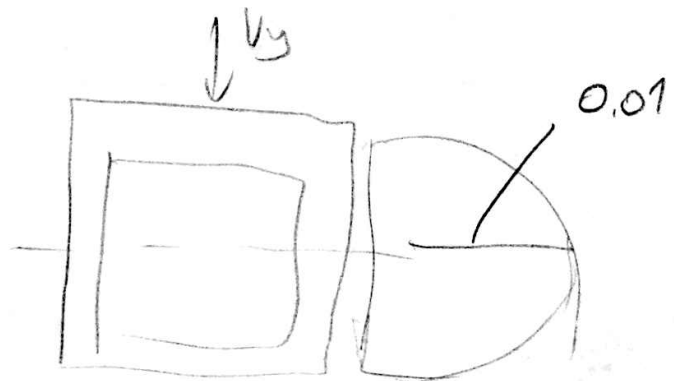
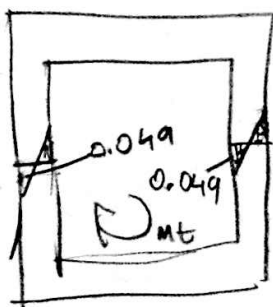
$$= 0.01 \text{ kN/mm}^2$$

$$I_{\text{TOTAL}} = \left[\frac{1}{12} 40 \cdot 10^3 + 400(39.14)^2 + (2) \frac{1}{12} \cdot 5 \cdot 85^3 + (2) 425 \cdot 5.86^2 + \frac{1}{12} 40 \cdot 5^3 + 200(53.36)^2 \right]$$

$$= 652775.84 + 546959.5 + 569874.59 + 1763609.93 \text{ mm}^4$$

$$Q = \sum Ay' = (2)(34.14)(5)(5.86) + (40)(10)(39.14) = 17,656.6 \text{ mm}^3$$

$$b = 2 \times 5 = 10 \text{ mm}$$



$$0.049 + 0.049 + 0.01 = 0.1089 \text{ kN/mm}^2$$