



Calculating Angles

$$\angle B A : \theta_1 + 90^\circ + \theta = 180^\circ$$

$$\Rightarrow \boxed{\theta_1 = 90^\circ - \theta}$$

$$\bullet \theta_1 + \theta_5 = 90^\circ \Rightarrow \theta_5 = 90^\circ - \theta_1 = 90^\circ - (90^\circ - \theta)$$

$$\Rightarrow \boxed{\theta_5 = \theta}$$

$$\angle O A : \theta_2 + 90^\circ + \theta = 180^\circ$$

$$\Rightarrow \boxed{\theta_2 = 90^\circ - \theta}$$

$$\theta_2 + \theta_3 = 90^\circ \Rightarrow \theta_3 = 90^\circ - \theta_2 = 90^\circ - (90^\circ - \theta) \Rightarrow \boxed{\theta_3 = \theta}$$

$$\angle A O : \theta_3 + 90^\circ + \theta_4 = 180^\circ \Rightarrow \theta_4 = 90^\circ - \theta_3 = 90^\circ - \theta$$

$$\Rightarrow \boxed{\theta_4 = 90^\circ - \theta}$$

Analysing Vectors

$$\cos(\theta_4) = \frac{W_T}{|\vec{W}|} \Rightarrow W_T = m \cdot g \cos(90^\circ - \theta)$$

$$\Rightarrow \boxed{W_T = m \cdot g \cdot \sin(\theta)}$$

$$\sin(\theta_4) = \frac{W_N}{|\vec{W}|} \Rightarrow W_N = m \cdot g \cdot \sin(90^\circ - \theta)$$

$$\Rightarrow W_N = -m \cdot g \cdot \sin(\theta - 90^\circ) \Rightarrow \boxed{W_N = -m \cdot g \cdot \cos(\theta)}$$

$$\vec{T} = T_O \hat{O} + T_N \hat{N}_O$$

$$\cos(\theta) = \frac{a_T}{|\vec{a}|} \Rightarrow \boxed{a_T = |\vec{a}| \cdot \cos(\theta)}$$

$$\sin(\theta) = \frac{a_N}{|\vec{a}|} \Rightarrow \boxed{a_N = |\vec{a}| \cdot \sin(\theta)}$$

Newton's Law

$$\Sigma F_T = m \cdot a_T \Rightarrow \cancel{T_N - m \cdot g \cdot \sin(\theta) = m \cdot |\vec{a}| \cdot \cos(\theta)}$$

$$\Rightarrow W_T = m \cdot a_T \Rightarrow m \cdot g \cdot \sin(\theta) = m \cdot |\vec{a}| \cdot \cos(\theta)$$

$$\Rightarrow |\vec{a}| = g \cdot \frac{\sin \theta}{\cos \theta} \Rightarrow \boxed{|\vec{a}| = g \cdot \tan(\theta)} \quad (1)$$

$$\Sigma F_N = m \cdot a_N \Rightarrow \cancel{T_N} - m \cdot g \cdot \cos \theta = m \cdot |\vec{a}| \cdot \sin(\theta)$$

$$\Rightarrow T_N = m \cdot |\vec{a}| \cdot \sin \theta + m \cdot g \cdot \cos \theta$$

$$\Rightarrow T_N = m \cdot g \cdot \tan(\theta) \cdot \sin \theta + m \cdot g \cdot \cos \theta$$

$$\Rightarrow \boxed{T_N = m \cdot g [\tan(\theta) \cdot \sin(\theta) + \cos(\theta)]} \quad (2)$$

$$a_N = |\vec{a}| \cdot \sin(\theta) = \overbrace{g \cdot \tan(\theta)}^{|\vec{a}|} \cdot \sin(\theta) = \frac{|\vec{v}|^2}{R=L}$$

$$\Rightarrow \boxed{|\vec{v}| = \sqrt{L \cdot g \cdot \tan(\theta) \cdot \sin(\theta)}}$$

~~$$|\vec{v}| = L \cdot \frac{d\theta}{dt} \Rightarrow \frac{d\theta}{dt} = \frac{|\vec{v}|}{L}$$~~

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$$|\vec{v}| = \omega \cdot L = \frac{\partial \theta}{\partial t} \cdot L \Rightarrow L = \frac{\partial \theta}{\partial t} \cdot L \cdot \frac{1}{|\vec{v}|}$$

$$\Rightarrow \frac{1}{L} = \frac{\partial \theta}{\partial t} \cdot \frac{1}{|\vec{v}|} \Rightarrow \frac{1}{L} \cdot \partial t = \frac{1}{|\vec{v}|} \cdot \partial \theta$$

$$\Rightarrow \frac{1}{L} \partial t = \frac{\partial \theta}{\sqrt{L \cdot g \cdot \tan \theta \cdot \sin \theta}}$$

$$\Rightarrow \frac{1}{L} \int_0^t 1 \cdot \partial t = \int_{\theta(0)}^{\theta(t)} \frac{\partial \theta}{\sqrt{L \cdot g \cdot \tan \theta \cdot \sin \theta}}$$

$$\Rightarrow \frac{1}{L} \cdot t = \int_{\theta(0)}^{\theta(t)} \frac{\partial \theta}{L \cdot g \cdot \tan(\theta) \cdot \sin(\theta)}$$

$$= \dots = \boxed{\theta(t) = \dots}$$